# Mark Scheme (Results) 

## January 2012

GCE Statistics S2 (6684) Paper 1

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.


## EDEXCEL GCE MATHEMATICS

## General Instructions for Marking

1. The total number of marks for the paper is 75 .
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes and can be used if you are using the annotation facility on ePEN.

- bod - benefit of doubt
- ft - follow through
- the symbol $\_$will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper
- The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

## General Principals for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

## Method mark for solving 3 term quadratic:

1. Factorisation

$$
\begin{aligned}
\left(x^{2}+b x+c\right) & =(x+p)(x+q), \text { where }|p q|=|c|, \text { leading to } x=\ldots \\
\left(a x^{2}+b x+c\right) & =(m x+p)(n x+q), \text { where }|p q|=|c| \text { and }|m n|=|a|, \text { leading to } x=\ldots
\end{aligned}
$$

2. Formula

Attempt to use correct formula (with values for $a, b$ and $c$ ), leading to $x=\ldots$
3. Completing the square

Solving $x^{2}+b x+c=0: \quad\left(x \pm \frac{b}{2}\right)^{2} \pm q \pm c, \quad q \neq 0, \quad$ leading to $x=\ldots$

## Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1. ( $x^{n} \rightarrow x^{n-1}$ )
2. Integration

Power of at least one term increased by 1. ( $x^{n} \rightarrow x^{n+1}$ )

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.
Normal marking procedure is as follows:
Method mark for quoting a correct formula and attempting to use it, even if there are mistakes in the substitution of values.
Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

## January 2012 <br> 6684 Statistics S2 <br> Mark Scheme



| Question Number | Scheme |  | Marks |
| :---: | :---: | :---: | :---: |
| 2 |  |  | B1 <br> B1 <br> M1 <br> M1 <br> A1 <br> M1 dep <br> A1 <br> (7) |
|  | Notes <br> $1^{\text {st }} \mathrm{B} 1$ for $\mathrm{H}_{0}: p=0.5$ <br> $2^{\text {nd }} \mathrm{B} 1$ for $\mathrm{H}_{1}: p>0.5$ <br> SC If both hypotheses are correct but a different letter to $p$ is used they get B1 B0. If no letter is used they get B0 B0. <br> $1^{\text {st }}$ M1 writing or using $B(30,0.5)$ <br> One tail <br> $\overline{2^{\text {nd }} \mathrm{M} 1}$ for writing or using $1-\mathrm{P}(X \leq 20)$ or writing $\mathrm{P}(X \leq 19)=0.9506$ or $\mathrm{P}(X \geq 20)=0.0494$. May be implied by correct CR.or probability $=0.0214$ <br> A1 for 0.0214 or $\mathrm{CR} X \geq 20 / X>19$. NB $\mathrm{P}(X \leq 20)=0.9786$ on its own scores M1A1 <br> $3^{\text {rd }}$ M1 dependent on the $2^{\text {nd }}$ M1 being awarded. For a correct statement based on the table below. Do not allow non-contextual conflicting statements eg "significant" and "accept $\mathrm{H}_{0}$ ". Ignore comparisons. <br> $2^{\text {nd }} \mathrm{A} 1$ for a correct contextualised statement. NB A correct contextual statement on its own scores M1A1. <br> $0.05<p<0.95$ $p<0.05$ or $p>0.95$ |  |  |
|  | Two tail <br> $1^{\text {st }} \mathrm{M} 1$ for writing or using $1-\mathrm{P}(X \leq 20)$ or writing $\mathrm{P}(X \leq 20)=0.9786$ or $\mathrm{P}(X \geq 21)=0.0214$. May be implied by correct CR. or probability $=0.197$ <br> A1 for 0.0214 or $\mathrm{CR} X \geq 21 / X>20$. NB $\mathrm{P}(X \leq 20)=0.9786$ on its own scores M1A1 $3^{\text {rd }}$ M1 dependent on the $2^{\text {nd }}$ M1 being awarded. For a correct statement based on the table below. Do not allow non-contextual conflicting statements eg"significant" and "accept $\mathrm{H}_{0}$ ". Ignore comparisons. <br> $2^{\text {nd }}$ A1 for a correct contextualised statement. NB A correct contextual statement on its own scores M1A1. |  |  |
| Question | Scheme |  | Marks |





| Question <br> Number | Scheme | Marks |
| :--- | :---: | :---: |



1st M1 $\int_{1}^{k} x-\frac{1}{2} \mathrm{~d} x=0.5$
or $\int_{1}^{k} x-\frac{1}{2} \mathrm{~d} x+0.5=1$
ignore limits
or $\int_{1}^{k} x-\frac{1}{2} \mathrm{~d} x+\int_{1}^{k} \frac{1}{2} \mathrm{~d} x=1$
or $\frac{1}{2}(k-0.5+0.5)(k-1)=0.5$ or any correct method of finding the area
1 st A1 for a quadratic equation in the form $a\left(k^{2}-k-1\right)=0$ or $a k^{2}-a k=a$. where $a$ is a constant.
$2^{\text {nd }}$ M1 correct method for solving a quadratic of the form $a k^{2}-b k+c=0$ where $a, b, c \neq 0$. There must be at least one correct step before the final answer. Allow substituting in $k$ into a quadratic of the form $a k^{2}-b k+c=0$.
$2^{\text {nd }} \mathrm{A} 1$ cso for $k=\frac{1}{2}(1+\sqrt{5})$
1st B1 for second line. Do not penalise the use of $<$ instead of $\leq$ and vice versa
M1 for use of $\int_{1}^{k} x-\frac{1}{2} \mathrm{~d} x+\mathrm{C}$ ignore limits. For use they must have $x \rightarrow x^{2}$
1 st A1 correct integration $\frac{1}{2} x^{2}-\frac{1}{2} x$
2nd A1 C $=\frac{1}{2}$
NB M1A1A1 may be implied by correct 3rd line in $\mathrm{F}(x)$
2nd B1 for 3rd line. Statement of the form $\frac{1}{2} x^{2}-\frac{1}{2} x \pm C$. Do not penalise the use of $<$ instead of $\leq$ and vice versa. Allow $k$ or value of $k$. $C$ may equal 0 .
3rd B1 for first and last line. Do not penalise the use of $\leq$ instead of $<$ and $\geq$ instead of >. Allow $k$ or value of $k$
(d) M1 Using $\mathrm{F}(1.5)-\mathrm{F}(0.5) .1 .5$ must be put into the third line of the c.d.f. and 0.5 must be put into the second line of the c.d.f..
or $\int_{0.5}^{1} \frac{1}{2} x \mathrm{~d} x+\int_{1}^{1.5} x-\frac{1}{2} \mathrm{~d} x$ need to attempt integration, at least one $x^{n} \rightarrow x^{n+1}$
or seeing $0.25+0.375$ or any correct method of finding the area..
(NB if they have not used +C or $\mathrm{C}=0$ they will get 0.125 . This will get M1A0). An answer of 0.125 from an incorrect method gains M0 A0.
(e) If it is not clear which one is the mode and which one is the median assume the median is the first answer and mode the second.
(f) $\quad$ B1 negative/negative skew(ness). Do not allow negative correlation.

B1 dependent on previous B mark being awarded. Reason must follow from their values or diagram.

| Question <br> Number | Scheme | Marks |
| :---: | :--- | :--- |
| $\mathbf{7 ( a ) ( i )}$ | The range of values/region/area/set of values of the test statistic that would lead you <br> to $\underline{\text { reject } \mathbf{H}_{0}}$ <br> (a) (ii) <br> The probability of incorrectly rejecting $\mathrm{H}_{0}$ or <br> Probability of rejecting $\mathrm{H}_{0}$ when $\mathrm{H}_{0}$ is true B1 |  |

(b) (i)
$X \sim \operatorname{Po}(8)$
$\mathrm{P}(X \leq 4)=0.0996$
$\mathrm{P}(X \leq 3)=0.0424$
(b) (ii)

Critical region [0,3]
awrt 0.0424
(c)
$\mathrm{H}_{0}: \lambda=8 \quad($ or $\mu=8)$
$\mathrm{H}_{1}: \lambda>8 \quad($ or $\mu>8)$
$\mathrm{P}(X \geq 13)=1-\mathrm{P}(X \leq 12)$
or $\mathrm{P}(X \leq 13)=0.9658$
$=1-0.9362$
$=0.0638$
CR $X \geq 14$
so insufficient evidence to reject $\mathrm{H}_{0} /$ not significant/ not in critical region
There in insufficient evidence of an increase/change in the rate/number of sales per
A1 month or the estate agents claim is incorrect

Allow accept $\mathrm{H}_{1}$ instead of reject $\mathrm{H}_{0}$. It must be clear which hypothesis gets rejected/accepted.
(c)

Allow equivalent wording.
M1 Writing or using $\operatorname{Po}(8)$. May be implied by correct critical region.
A1 allow $0 \leq X \leq 3$ or $\mathrm{CR} \leq 3$ or $X \leq 3$. Any letter may be used but not $\mathrm{P}(X \leq 3)$. This must be on its own.
B1 both hypotheses correct. Must use $\lambda$ or $\mu$.
One tail
$1^{\text {st }} \mathrm{M} 1$ for writing or using $1-\mathrm{P}(X \leq 12)$ or writing $\mathrm{P}(X \leq 13)=0.9658$ or $\mathrm{P}(X \geq 14)=0.0342$. May be implied by correct CR.or probability $=0.0638$
A1 for 0.0638 or $X \geq 14$. Allow $X>13$. NB $\mathrm{P}(X \leq 12)=0.9362$ on its own scores M1A1
$2^{\text {nd }}$ M1 dependent on the $1^{\text {st }}$ M1 being awarded. For a correct statement based on the table below. Do not allow noncontextual conflicting statements eg "not significant" and "reject $\mathrm{H}_{0}$ ". Ignore comparisons.
$2^{\text {nd }} \mathrm{A} 1$ for a correct contextualised statement. NB A correct contextual statement on its own scores M1A1.

|  | $0.05<p<0.95$ | $p<0.05$ or $p>0.95$ |
| :--- | :--- | :--- |
| $2^{\text {nd }} \mathrm{M} 1$ | not significant/ accept $\mathrm{H}_{0} /$ Not in CR | significant/reject $\mathrm{H}_{0} /$ In CR |
| $2^{\text {nd }} \mathrm{A} 1$ | Insufficient evidence of an increase/change in the <br> rate/number | Sufficient evidence of an increase/change in the <br> rate/number of sales per month |

## Two tail

$1^{\text {st }} \mathrm{M} 1$ for writing or using $1-\mathrm{P}(X \leq 12)$ or writing $\mathrm{P}(X \leq 14)=0.9827$ or $\mathrm{P}(X \geq 15)=0.0173$. May be implied by correct CR.or probability $=0.0638$
A1 for 0.0638 or $X \geq 15$. Allow $X>14$. NB $\mathrm{P}(X \leq 12)=0.9362$ on its own scores M1A1
$2^{\text {nd }}$ M1 dependent on the $1^{\text {st }}$ M1 being awarded. For a correct statement based on the table below. Do not allow noncontextual conflicting statements eg "not significant" and "reject $\mathrm{H}_{0}$ ". Ignore comparisons.
$2^{\text {nd }} \mathrm{A} 1$ for a correct contextualised statement. NB A correct contextual statement on its own scores M1A1.

|  | $0.025<p<0.975$ | $p<0.025$ or $p>0.975$ |
| :--- | :--- | :--- |
| $2^{\text {nd }} \mathrm{M} 1$ | not significant/ accept $\mathrm{H}_{0} /$ Not in CR | significant/reject $\mathrm{H}_{0} /$ In CR |
| $2^{\text {nd }} \mathrm{A} 1$ | Insufficient evidence of an increase/change in the <br> rate/number of sales per month | Sufficient evidence of an increase/change in the <br> rate/number of sales per month |

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